

Mass Parabolas and Stability

$$M(A, Z) = \alpha + \beta Z + \gamma Z^2$$

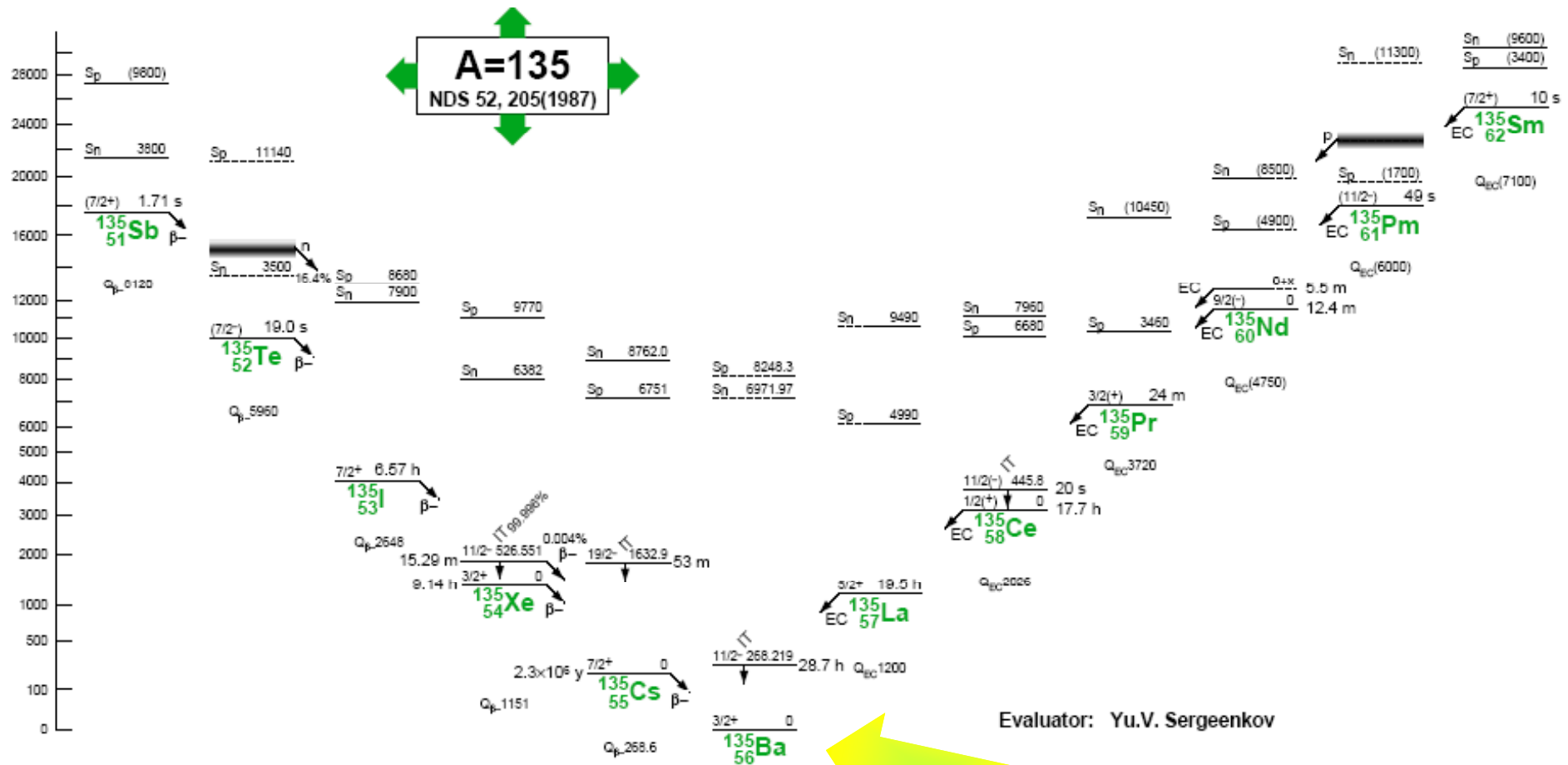
$$\alpha = AM_n - a_v A + a_s A^{2/3} + a_a A - \delta - \eta$$

$$\beta = -(M_n - M_H) - a_c A^{-1/3} - 4a_a$$

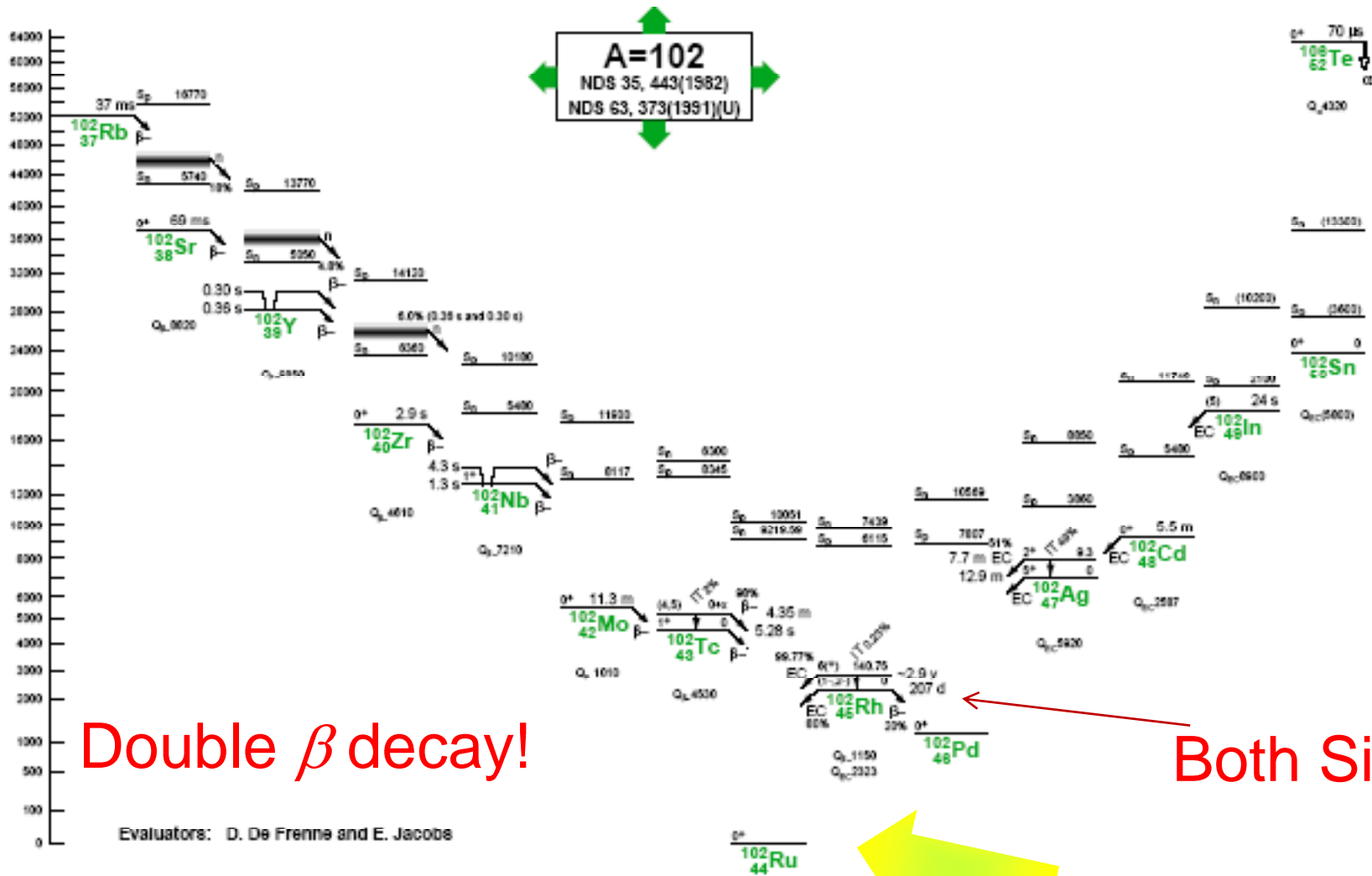
$$\gamma = 4a_a A^{-1} + a_c A^{-1/3}$$

$$\left. \frac{\partial M}{\partial Z} \right|_A = 0 \Rightarrow Z_{\min} = -\frac{\beta}{2\gamma}$$

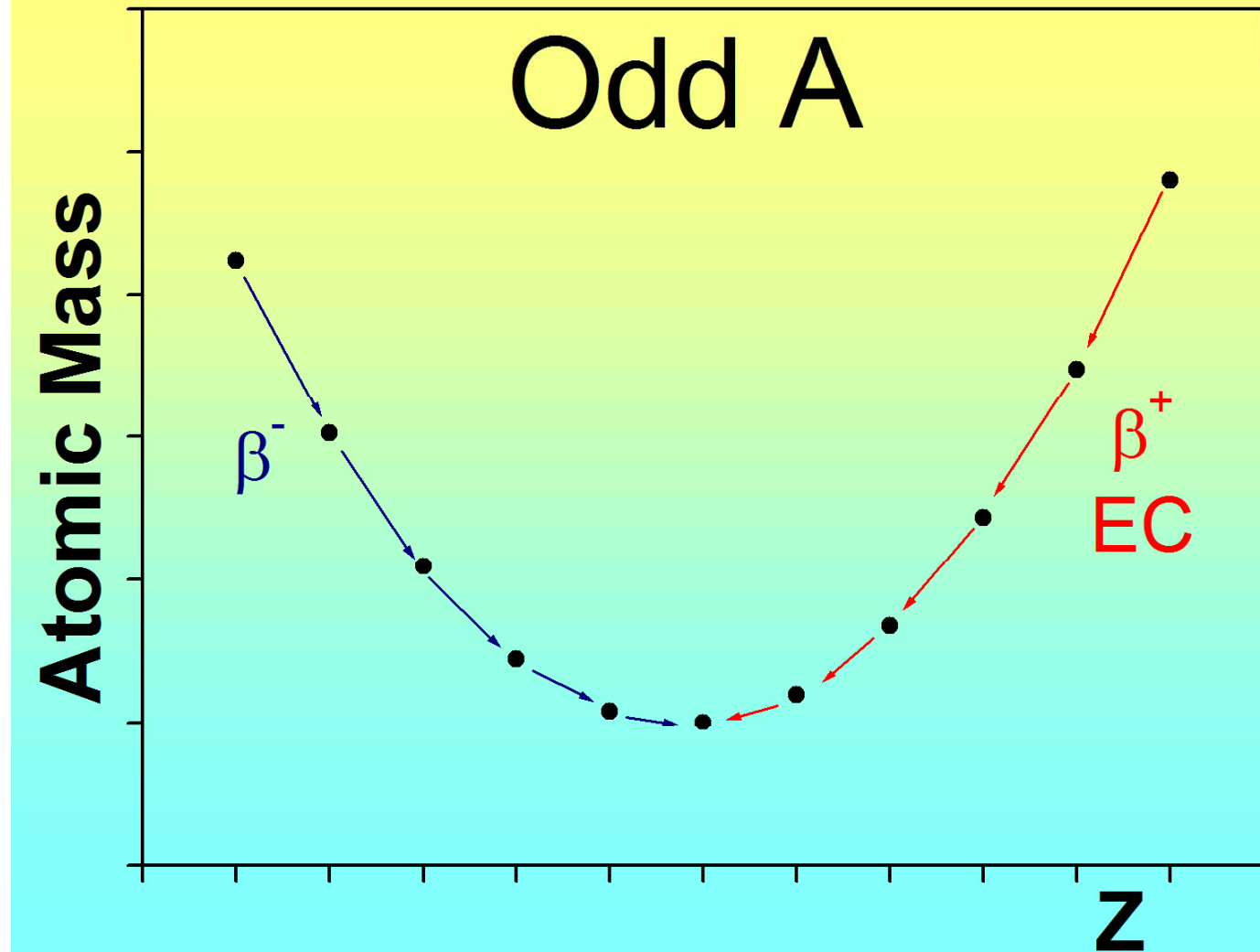
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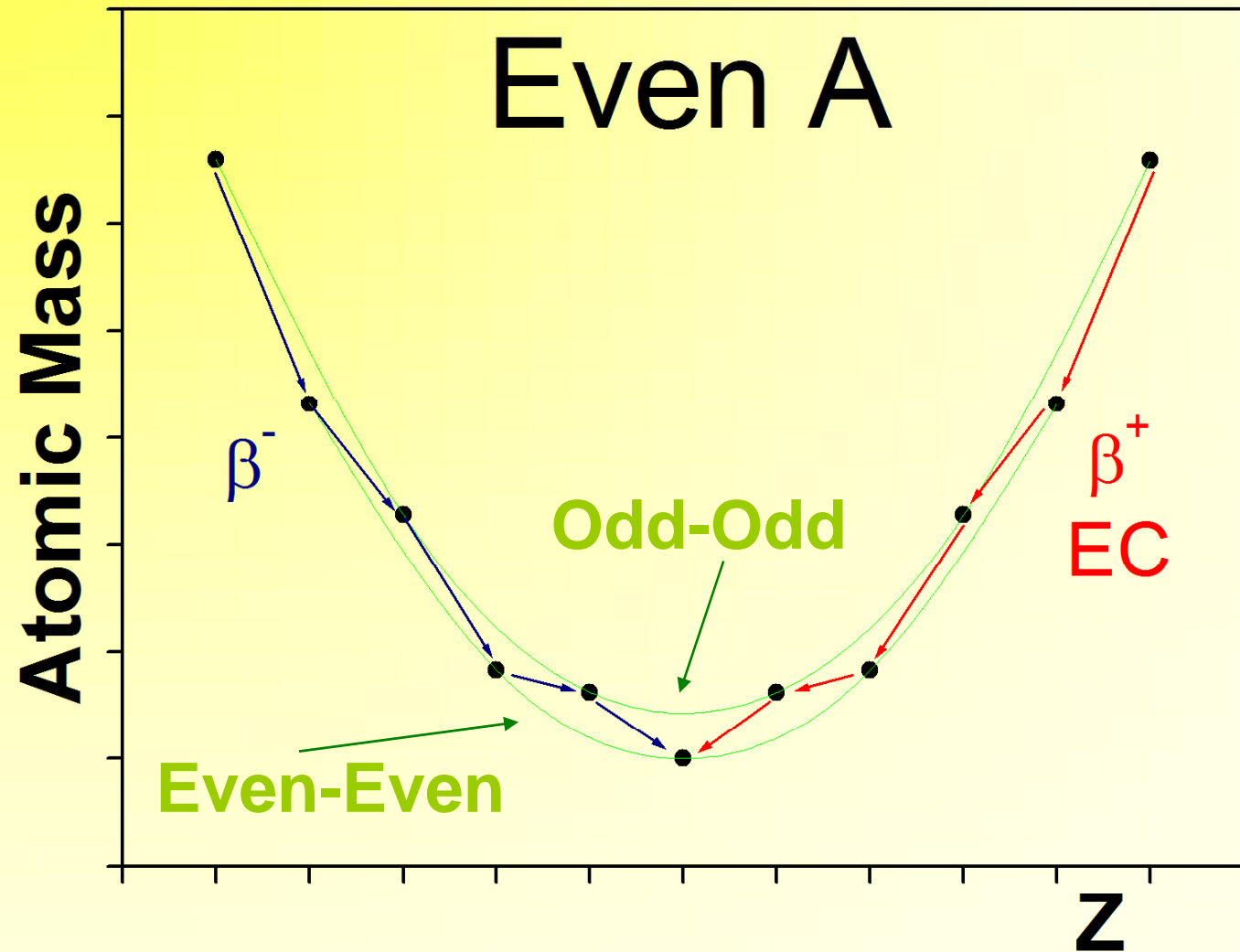


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Vertical spacing between both parabolas ?



Nuclear Spin

- Neutrons and protons have $s = \frac{1}{2}$ ($m_s = \pm \frac{1}{2}$) so they are fermions and obey the Pauli-Exclusion Principle.
- The Pauli-Exclusion Principle applies to neutrons and protons separately (distinguishable from each other) (**Isospin**).
- Nucleus seen as single entity with **intrinsic angular momentum I (or J)**.
- Associated with each nuclear spin is a **nuclear magnetic moment** which produces magnetic interactions with its environment.
- The suggestion that the angular momenta of nucleons tend to form pairs is supported by the fact that all nuclei with even Z and even N have nuclear spin $I=0$.
- Iron isotopes (even-Z), for even-N (even-A) nuclei $I=0$.
- Odd-A \blacktriangleright contribution of odd neutron \blacktriangleright half-integer spin.
- Cobalt (odd-Z), for even-N \blacktriangleright contribution of odd proton \blacktriangleright half-integer spin.
- Odd-N \blacktriangleright two unpaired nucleons \blacktriangleright large integer spin.

Nuclear Spin

Z	A	Spin	Natural Abundance	Half-life	Decay
26	54	0	0.059	stable	...
26	55	3/2	...	2.7y	EC
26	56	0	0.9172	stable	...
26	57	1/2	0.021	stable	...
26	58	0	0.0028	stable	...
26	60	0	...	1.5My	β^-

Nuclear Spin

Z	A	Spin	Natural Abundance	Half-life	Decay
27	56	4	...	77.7d	β^+
27	57	7/2	...	271d	EC
27	59	7/2	1.00	stable	...
27	60	5	...	5.272y	β^-